

# Multiagent Systems

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**Introduction**

Distributed Sensors Example

Coalition Formation Example

Distributed Resource Allocation

Conclusion

# Multiagent Systems

Engineer systems composed of  
**autonomous** and **localized**  
entities.

# Ongoing Trends

- ▶ Internet.
- ▶ Mobile. Ubiquity.
- ▶ Delegation. Automation. Online interactions.
- ▶ Agent intelligence.

# Examples



CaseFetch™



ItemFetch™

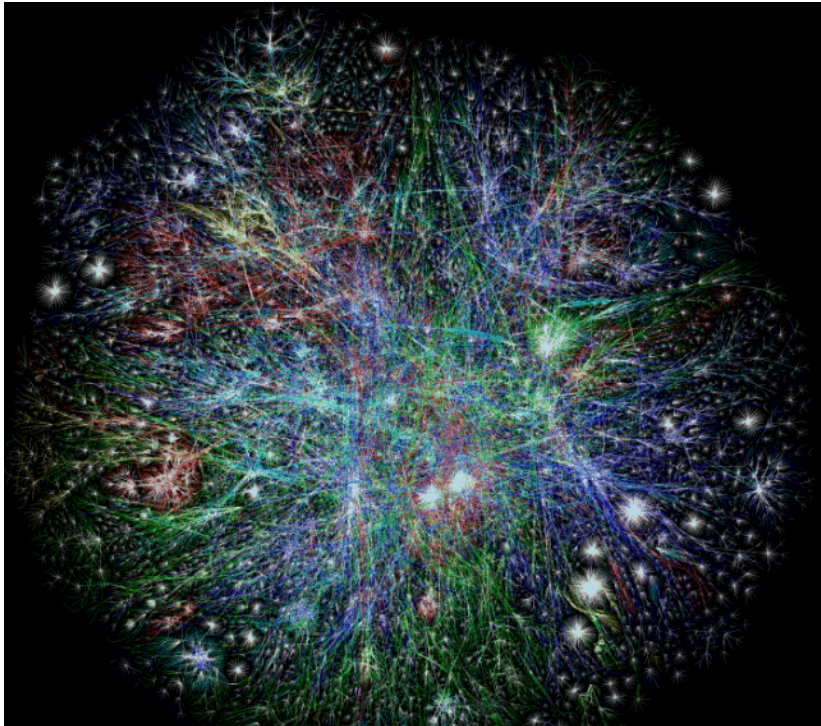


OrderFetch™

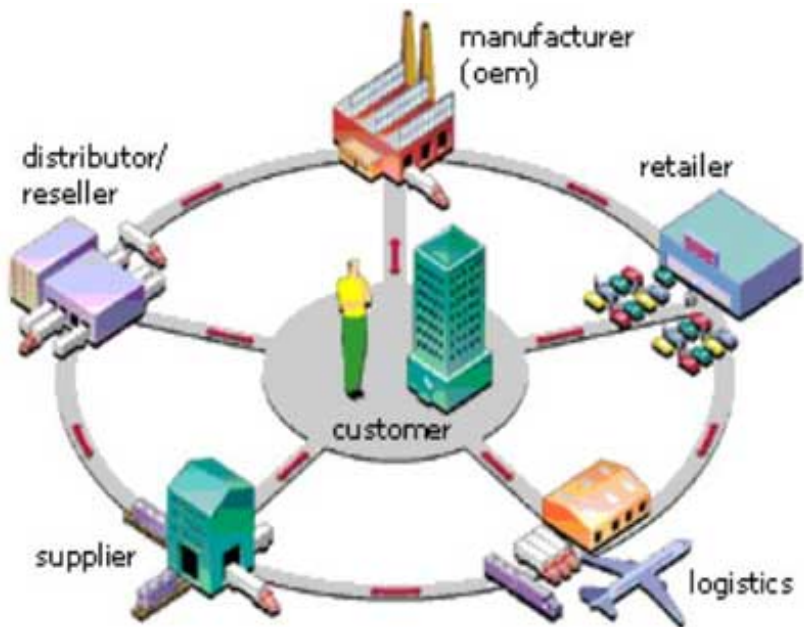












# Tools

- ▶ AI, Algorithms
- ▶ Economics, Game Theory, Algorithmic Game Theory

Introduction

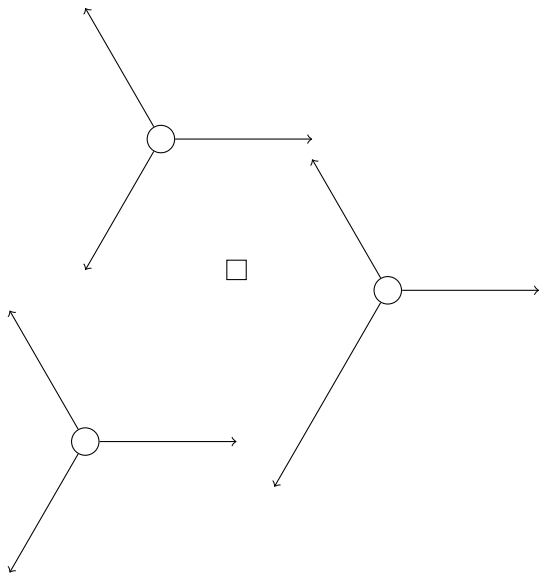
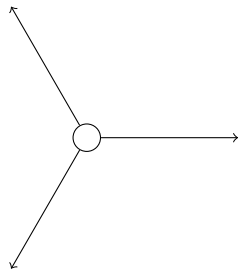
**Distributed Sensors Example**

Coalition Formation Example

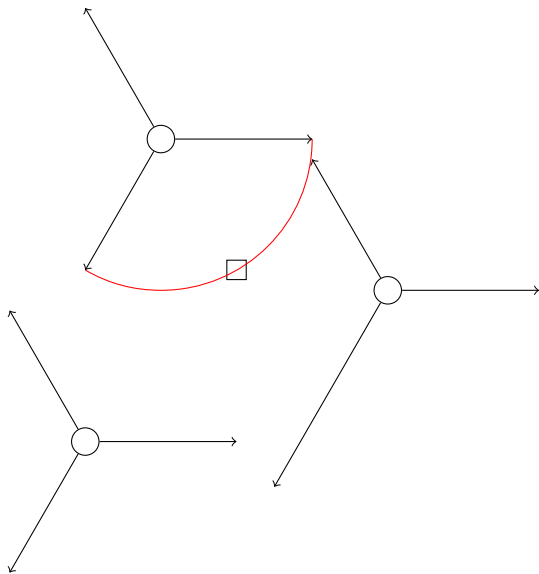
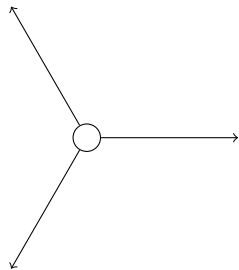
Distributed Resource Allocation

Conclusion

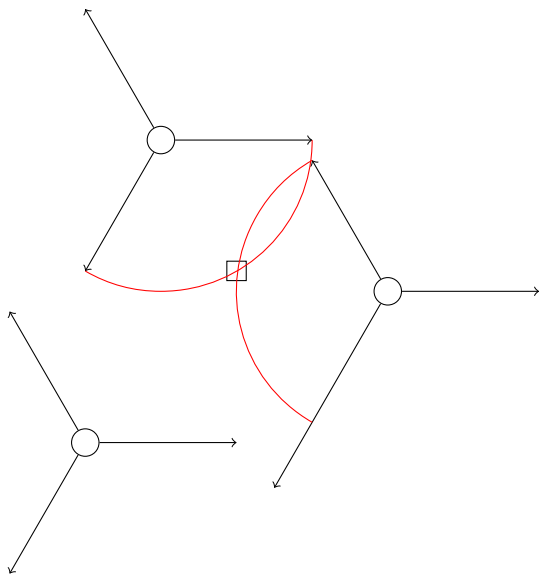
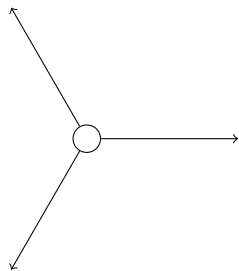
# Distributed Sensor Network



# Distributed Sensor Network

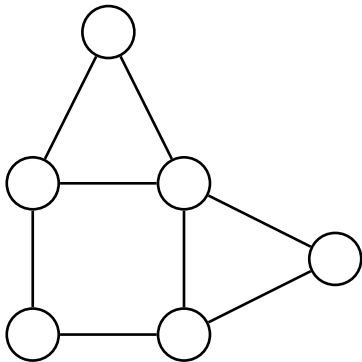


# Distributed Sensor Network

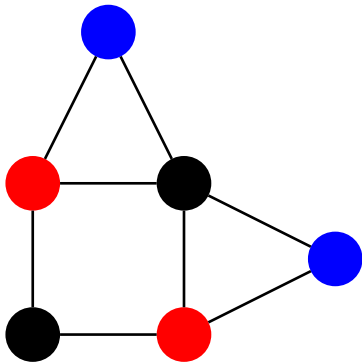




## Graph Coloring



# Graph Coloring



## Distributed Constraint Satisfaction Problem (DCSP)

Given variables  $x_1, x_2, \dots, x_n$ , each one controlled by a different agent, with domains  $D_1, D_2, \dots, D_n$  and a set of boolean constraints  $P$  of the form  $pk(x_{k1}, x_{k2}, \dots, x_{kj}) \rightarrow \{0, 1\}$ , find assignments for all the variables such that no constraints are violated.

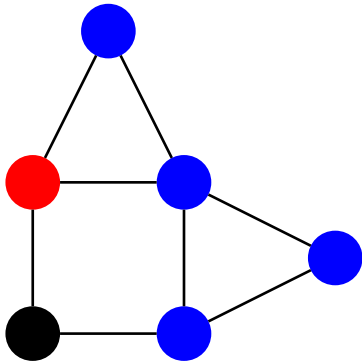
# Algorithms

- ▶ Filtering algorithm
- ▶ Hyper-Resolution Based Consistency algorithm
- ▶ Asynchronous Backtracking
- ▶ Asynchronous Weak-Commitment Search
- ▶ Distributed Breakout

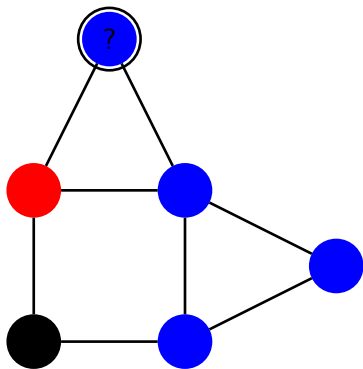
# Algorithms

- ▶ Filtering algorithm **NOT Complete**
- ▶ Hyper-Resolution Based Consistency algorithm **Complete**
- ▶ Asynchronous Backtracking **Complete**
- ▶ Asynchronous Weak-Commitment Search **Complete**
- ▶ Distributed Breakout **NOT Complete**

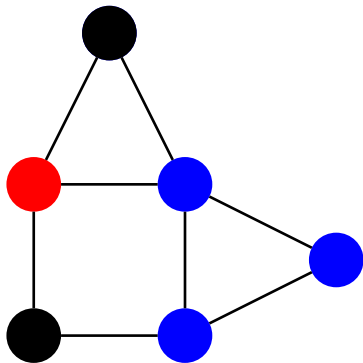
## Hill Climbing



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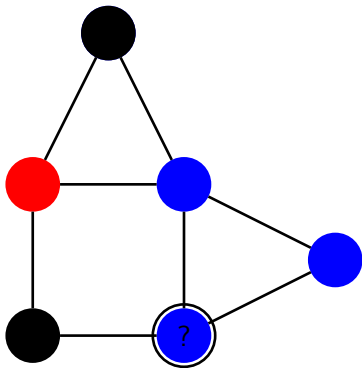


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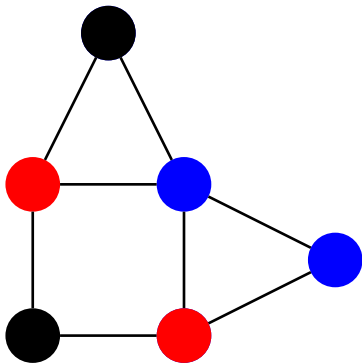




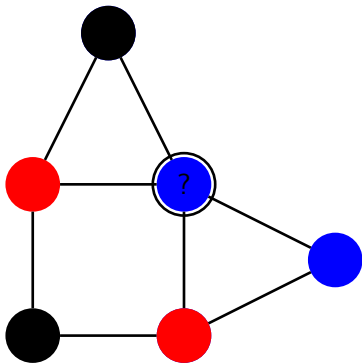
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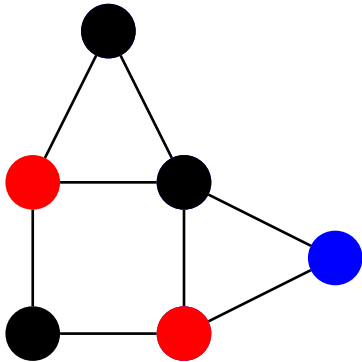
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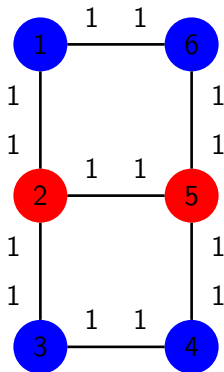
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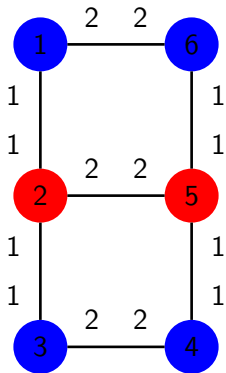
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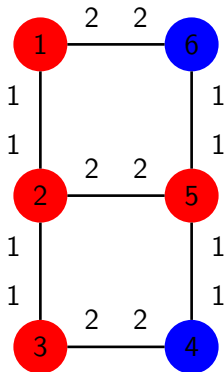
# Distributed Breakout



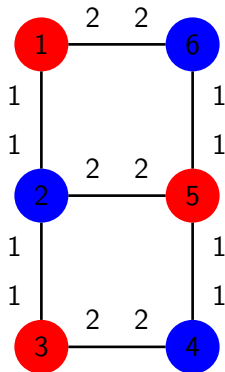
# Distributed Breakout



# Distributed Breakout



# Distributed Breakout





## Distributed Constraint Optimization Problem (DCOP)

Given variables  $x_1, x_2, \dots, x_n$ , each one controlled by a different agent, with domains  $D_1, D_2, \dots, D_n$  and a set of constraints  $P$  of the form  $pk(x_{k1}, x_{k2}, \dots, x_{kj}) \rightarrow \mathfrak{R}$ , find assignments for all the variables such that the sum of the constraint values is minimized.

# Algorithms

- ▶ Adopt
- ▶ OptAPO

# Completeness vs Speed vs Distribution

# Added Complications of Distributed Sensor Networks

- ▶ Noise
- ▶ Minimize communication
- ▶ Continuous problem

Introduction

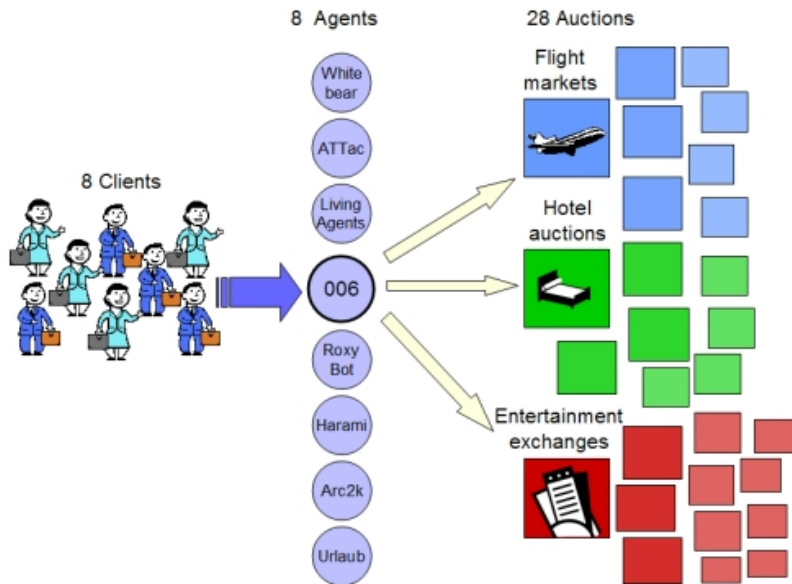
Distributed Sensors Example

**Coalition Formation Example**

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# Travel Software Agents



# Characteristic Form Game

$S$	$v(S)$
$(a)$	1
$(b)$	2
$(c)$	2
$(ab)$	4
$(ac)$	3
$(bc)$	4
$(abc)$	6

$$(a)(b)(c) \\ 1 + 2 + 2 = 5$$

$$(a)(bc) \\ 1 + 4 = 5$$

$$(b)(ac) \\ 2 + 3 = 5$$

$$(c)(ab) \\ 2 + 4 = 6$$

$$(abc) \\ 6$$

# The Core

## Definition (Core)

An outcome  $\mathbf{u}$  is in the *core* if

1.

$$\forall SCA : \sum_{i \in S} \mathbf{u}_i \geq v(S)$$

2. it is feasible.



## Characteristic Form Game

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$$(abc) \\ 6$$

$\mathbf{u} = \{2, 3, 2\}$  in core?

## Characteristic Form Game

$S$	$v(S)$			
$(a)$	1		$(a)(b)(c)$	
$(b)$	2		$1 + 2 + 2 = 5$	
$(c)$	2	$(a)(bc)$	$(b)(ac)$	$(c)(ab)$
$(ab)$	4	$1 + 4 = 5$	$2 + 3 = 5$	$2 + 4 = 6$
$(ac)$	3			
$(bc)$	4		$(abc)$	
$(abc)$	6		6	

$\mathbf{u} = \{2, 3, 2\}$  in core? **no, not feasible**

## Characteristic Form Game

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$$(abc) \\ 6$$

$\mathbf{u} = \{2, 2, 2\}$  in core? **yes**

## How do we Distribute Value?

- ▶ If they form (12), how much should each get paid?

$S$	$v(S)$
()	0
(1)	1
(2)	3
(12)	6

## Definition (Shapley Value)

Let  $B(\pi, i)$  be the set of agents in the agent ordering  $\pi$  which appear before agent  $i$ . The *Shapley value* for agent  $i$  given  $A$  agents is given by

$$\phi(i, A) = \frac{1}{A!} \sum_{\pi \in \Pi_A} v(B(\pi, i) \cup i) - v(B(\pi, i)),$$

where  $\Pi_A$  is the set of all possible orderings of the set  $A$ .

## How do we Distribute Value?

- ▶ If they form (12), how much should each get paid?

$S$	$v(S)$
$()$	0
$(1)$	1
$(2)$	3
$(12)$	6

$$\begin{aligned}\phi(1, \{1, 2\}) &= \frac{1}{2} \cdot (v(1) - v()) + v(21) - v(2)) \\ &= \frac{1}{2} \cdot (1 - 0 + 6 - 3) = 2 \\ \phi(2, \{1, 2\}) &= \frac{1}{2} \cdot (v(12) - v(1) + v(2) - v()) \\ &= \frac{1}{2} \cdot (6 - 1 + 3 - 0) = 4\end{aligned}$$

# Solutions

## From Game Theory:

- ▶ Core
- ▶ Nucleolus
- ▶ Shapley value

## From Sociology

- ▶ Equi-resistance
- ▶ Power-Dependence
- ▶ Expect Value



# Solutions

## From Game Theory:

- ▶ Core
- ▶ Nucleolus
- ▶ Shapley value

## From Sociology

- ▶ Equi-resistance
- ▶ Power-Dependence
- ▶ Expect Value

How to compute these? Distributedly.

# Distributed Search

FIND-COALITION( $i$ )

- 1  $L_i \leftarrow$  set of all coalitions that include  $i$ .
- 2  $S_i^* \leftarrow \arg \max_{S \in L_i} v_i(S)$
- 3  $w_i^* \leftarrow v_i(S_i^*)$
- 4 Broadcast  $(w_i^*, S_i^*)$  and wait for all other broadcasts.  
Put into  $W^*, S^*$  sets.
- 5  $w_{\max} = \max W^*$  and  $S_{\max}$  is the corresponding coalition.
- 6 **if**  $i \in S_{\max}$
- 7     **then** join  $S_{\max}$
- 8 Delete  $S_{\max}$  from  $L_i$ .
- 9 Delete all  $S \in L_i$  which include agents from  $S_{\max}$ .
- 10 **if**  $L_i$  is not empty
- 11     **then** goto 2
- 12 **return**

## Added Complications of Real-World Coalition Formation

- ▶ Uncertain knowledge
- ▶ Distributed incentive-compatible algorithms
- ▶ Speed! Approximation algorithms needed.

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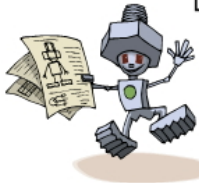
# TAC/SCM Scenario



**Suppliers**  
- strict MTO  
- variable supply and prices

Offers

**Agent**  
- automated  
- optimizing

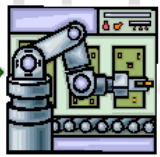


RFQs & orders

Production schedule

Delivery schedule

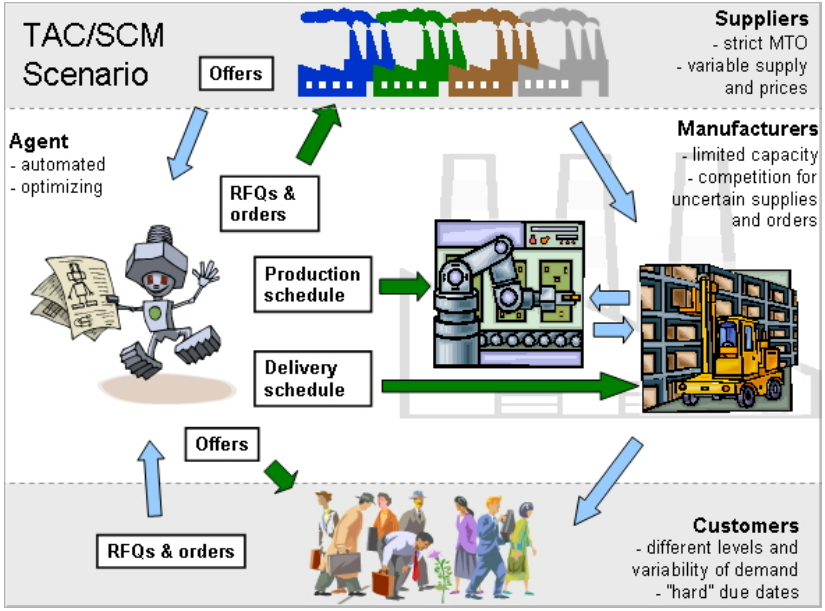
**Manufacturers**  
- limited capacity  
- competition for uncertain supplies and orders



Offers

RFQs & orders

**Customers**  
- different levels and variability of demand  
- "hard" due dates



# Combinatorial Auction



Bid Price	Bid items
\$1	Beast Boy
\$3	Robin
\$5	Raven, Starfire
\$6	Cyborg, Robin
\$7	Cyborg, Beast Boy
\$8	Raven, Beast Boy

# It is Hard

## Theorem

*Winner Determination in Combinatorial Auction is NP-hard. That is, finding the  $X^*$  that maximizes revenue is NP-hard.*

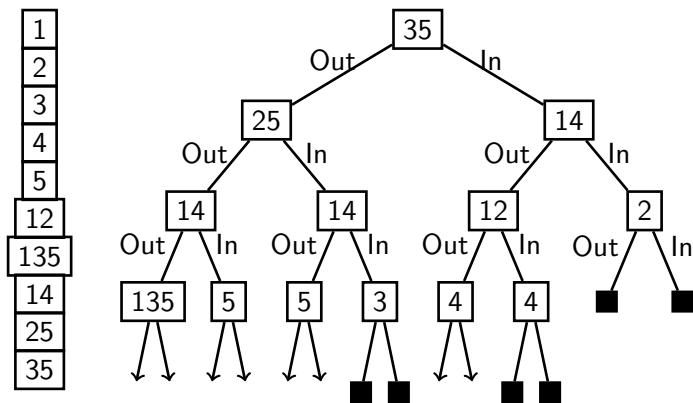
# It is Really Hard

## Theorem

*The decision version of the winner determination problem in combinatorial auctions is NP-complete, even if we restrict it to instances where every bid has a value equal to 1, every bidder submits only one bid, and every item is contained in exactly two bids.*



## Branch on Bids Search Tree



# Centralized Winner Determination Algorithms

- ▶ Results depend a lot on bid distribution and correlation.
- ▶ Thousands of bids doable in seconds.
- ▶ Newer algorithms use many different heuristics.
- ▶ Approximation algorithms are 1-2 orders faster but find only 99% of optimal solution.

## PAUSE Auction

- 1 Have simultaneous open-cry auctions for each individual item.
- 2 **For** ( $k \leftarrow 2; k \leq m; k \leftarrow k + 1$ )
- 3     **do** Each bidder must place a complete bidset  
      (using his bids or others' bids)  
      where bids are all of size less than  $k$ .

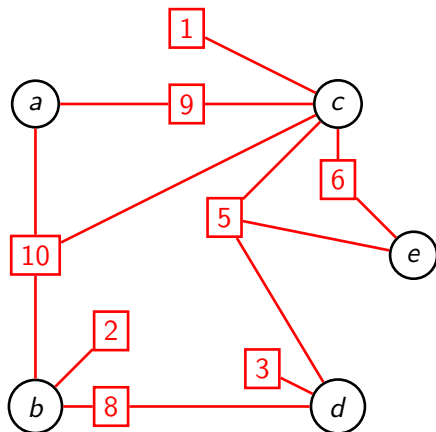
## PAUSE Bidding

- ▶ PAUSEBID: myopically-optimal bidding algorithm.
- ▶ PAUSE+PAUSEBID  $\rightarrow$  social welfare maximization, usually.

## Distribute Over Sellers

- ▶ Each seller of an item negotiates with other sellers to clear a bid for himself.
- ▶ We then have a **negotiation network**.

# Negotiation Network



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# Conclusion

## TOOLS:

- ▶ AI + Algorithms + Economics + Game Theory (Algorithmic Game Theory)

## GOALS:

- ▶ Engineer systems composed of **autonomous** and **localized** entities.